

# From Pixels to Purchases

A Deep Learning Approach to Heterogenous Consumer Aesthetics in Retail Fashion

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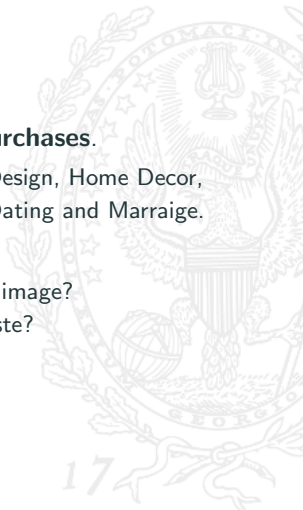
# Introduction

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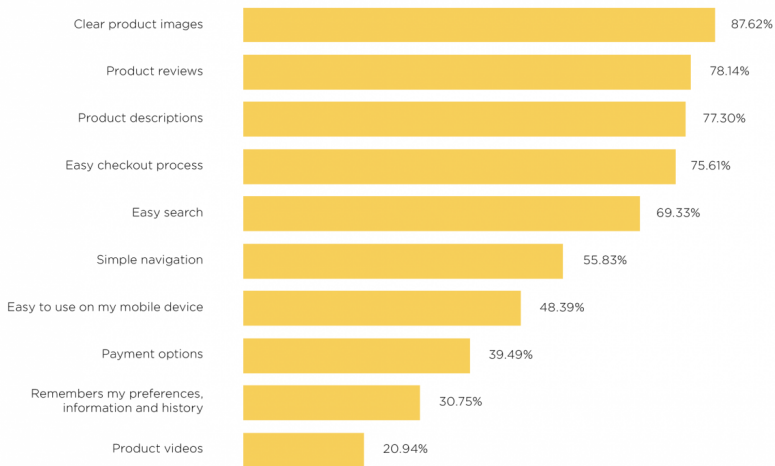
# Research Questions

- In some markets, **product aesthetics drives purchases.**
  - Fashion and Apparel, Designer Bags, Interior Design, Home Decor, Watches, Jewellery, Art, Luxury Cars, Shoes, Dating and Marriage.
- **Research Questions:**
  - How do we extract product aesthetics from an image?
  - How can we capture a diversity of aesthetic taste?
  - Will this change estimates of price sensitivity?
  - Can AI design new aesthetics?



# Motivation

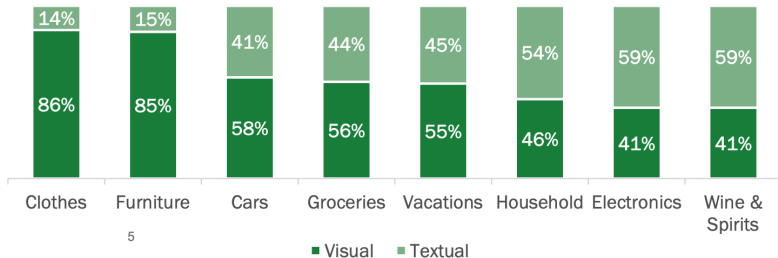
## Survey<sup>1</sup>: What makes for a great shopping experience?



<sup>1</sup>Namogoo 2018 Survey: A national sample of 1,372 U.S. online shoppers.

2018 Survey<sup>2</sup>: What is important when searching for a product online?

## Visual or Text Information Importance

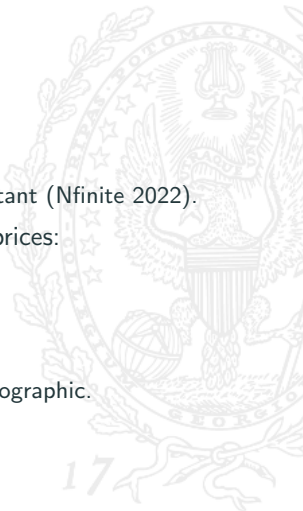


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<sup>2</sup>Intent Lab, Northwestern U: A national sample of 1000 U.S. residents.

Why should we care about images?

- Consumers care a lot about them.
  - 88% say high-quality product imagery is important (Nfinite 2022).
- Help us understand how consumers respond to prices:
  - By controlling for confounders.
  - By building instruments.
- **They are also interesting in their own right:**
  - For understanding the aesthetic taste of a demographic.
  - For developing and testing new designs.



Only recently<sup>3</sup>, some papers use images to estimate **price sensitivity**:

- Quah & Williams (2021): Logit-demand for shoes using images and debiased machine learning.
- Giovanni et al., (2021): Similarity between Amazon product webpages used to model error covariances in a nested logit.
- Han et al., (2021): Demand for fonts using dense embeddings from image autoencoders.

Other papers also use high dimensional information:

- Magnolfi et al., (2022): Demand estimation for cereal with tSNE embeddings of product characteristics from consumer surveys.
- Zhang (2024): Differentiates consumer price sensitivities by browsing activity in a market for smartphones.

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<sup>3</sup>Image processing only took off in 2014, high dim econometrics after 2016.

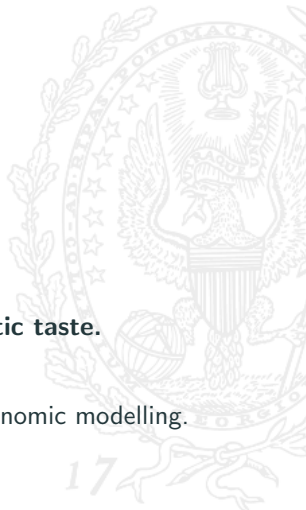


Two main limitations:

- No individual consumer heterogeneity.
- Focus has been mainly on price sensitivity.

The **contribution** of this project:

- **Modelling the variation in consumer aesthetic taste.**
- Estimating individual level price sensitivities.
- Showing how deep learning can be useful to economic modelling.



The methodology for this project is derived from:

- **Farrell et al. (2018, 2021): Neural networks can be used to model parameters and test hypotheses.**
- Chernozhukov et al. (2018, 2022): Sample-splitting can eliminate bias due to the use of regularized machine learning methods.
- Berry and Haile (2021), Ken Train (2009), Russell (2015): Surveys on demand estimation, discrete choice, and brand choice.
- Ludwig & Mullainathan (2023): Hypothesis generation through machine learning methods.

# Data

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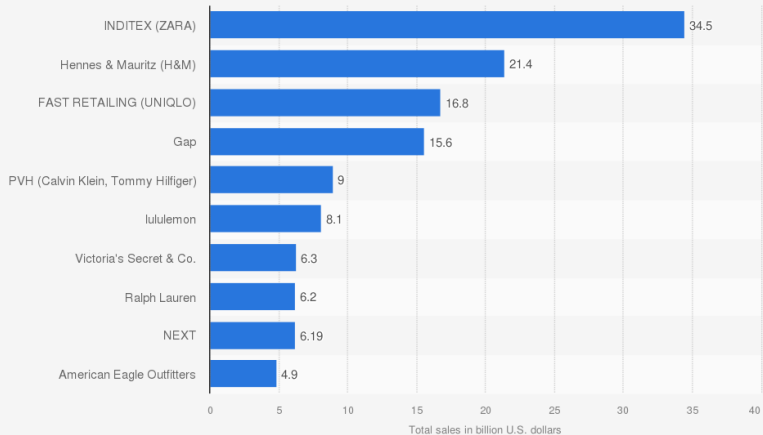


- Hennes & Mauritz (H&M) is a Swedish **fast fashion** brand:
  - 75 geographical markets
  - 4800 stores
  - 107,000 employees
  - 24.8 Billion USD annual revenue
- Motto: “to make fashion accessible and enjoyable for all”
  - Runway to store in 2 weeks.
- **Trendy and affordable clothes of lower quality.**



# Industry Snapshot

**Sales of major apparel manufacturers and retailers worldwide in the fiscal year 2022  
(in billion U.S. dollars)**



**Source**  
Fast Retailing  
© Statista 2024

**Additional Information:**  
Worldwide; 2022

# Data Summary

- Sample of **two years of shopping transactions** in an undisclosed European market (possibly the Netherlands):
  - 1,371,980 Customers
    - Median age 32, 66% Active
  - 108,775,015 Granular Products<sup>4</sup>.
    - Ladieswear (25%), Divided (14%), Menswear (12%)...
    - Trousers (11%), Dress (10%), Sweater (9%)...
    - 45875 products, **43404 text descriptions**
  - 31,788,324 Transactions
    - 70% offline, 30% online
- **Women's Dresses:** Popular category that has a large number of products with a wide range of distinct SKUs (2300).

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<sup>4</sup>Stock Keeping Units (SKUs)

# Dresses: Best Sellers

ID: 745475001  
Share: 0.38%



Short dress in woven fabric with a small stand-up collar and V-neck opening at the top. Dropped shoulders, short sleeves and a rounded hem. Slightly longer at the back.

ID: 817353008  
Share: 0.37%



Short dress in woven fabric with a V-neck, buttons down the front, short puff sleeves with smocked trims and a seam at the waist. Unlined.

ID: 745475002  
Share: 0.35%

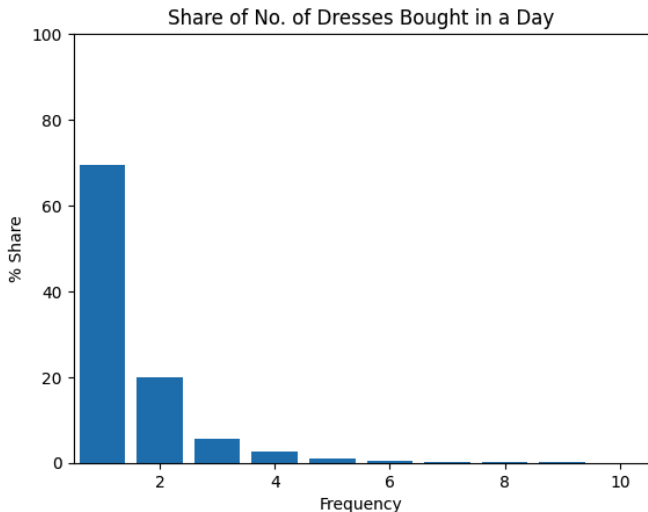


Short dress in woven fabric with a small stand-up collar and V-neck opening at the top. Dropped shoulders, short sleeves and a rounded hem. Slightly longer at the back.

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# Dresses: Purchases Per Day

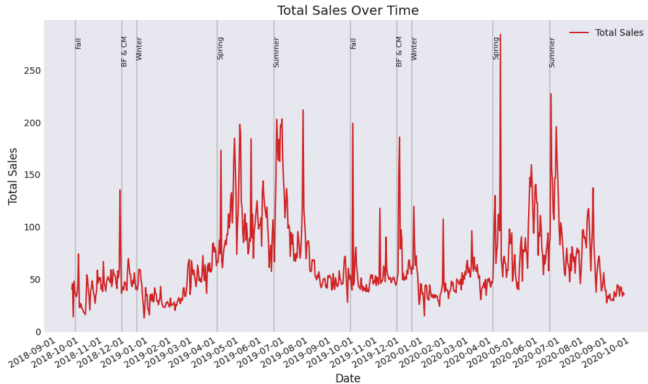
Majority of shoppers buy only one dress in a session.





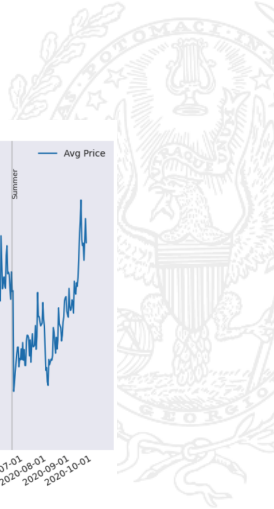
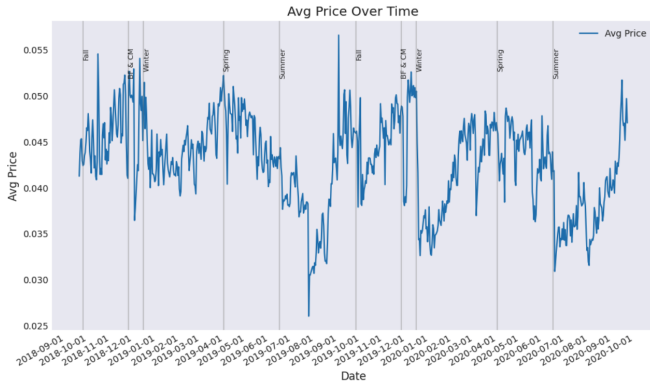
# Dresses: Sales over Time

- Strong seasonal variations
- Skewed: few products gather the most sales.



# Dresses: Avg Price over Time

- Sharp price discounting.
- Bell shaped prices.

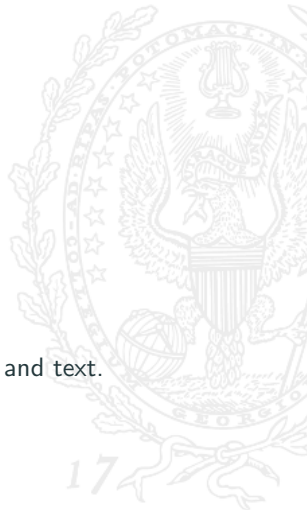


# Main Takeaways

The data suggests that:

- Discrete choice framework is appropriate.
- Images matter, at least for online shopping.
- Seasonal variation matters.

In the next section, I show how to work with images and text.



## Representing Images and Text

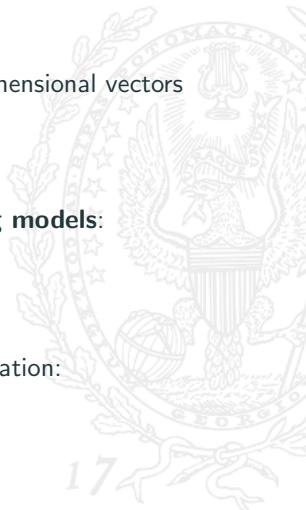
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# Embeddings

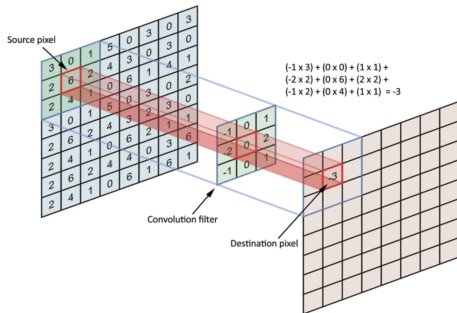
We can represent images and text by dense, high dimensional vectors called **embeddings**:

- We can estimate these embeddings ourselves.
- However, better to use **pre-trained embedding models**:
  - More parameters
  - More data
  - More training time
- I validate the usefulness of embedding representation:
  - They can help us predict prices and sales.
  - They cluster the product space intuitively.



# Embedding Images: Convolution Operator

A  $3 \times 128 \times 128$  image  $M_j$  has 49152 pixels for product  $j$ . A regression like  $s_j = \beta' M_j$  does not work because interactions between pixels matter<sup>5</sup>.

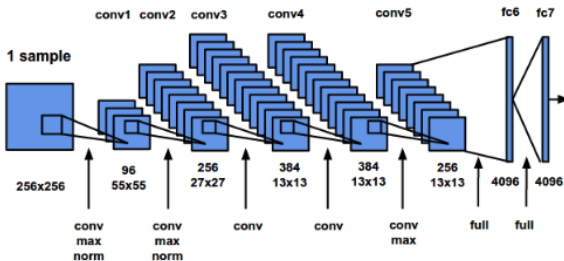


The convolution operator allows **parameter sharing** and captures **visual concepts** from **local spatial interactions** between pixels.

<sup>5</sup>With full interactions we get 1,207,984,128 parameters.

# Embedding Images: Conv-Net Architecture

Different **filters** extract different aspects of the image (e.g., shape, texture, pattern, etc.) and refine them into higher-level concepts.



The final output is a dense high-dimensional embedding  $e(M_j) \in \mathbb{R}^K$  that represents the attributes from the image<sup>6</sup>.

<sup>6</sup>Can be refined even further.

# Embedding Images: Image Regression

Estimate CNN on raw image pixels  $M_j$  to predict sales share  $s_j$ :

$$s_j = g^{\text{CNN}}(M_j) + \epsilon_j$$

and get an out-of-sample R2 of approximately 0.35.

Original Image - Pred Share: 0.024%



Round Neck - Pred Share: 0.020%



Sleeveless - Pred Share: 0.032%



Manually changing images, changes the prediction.



# Contrastive Language-Image Pre-training (CLIP)

- I use **Fashion CLIP**<sup>7</sup>, a model that matches image-text pairs to other image-text pairs that fall under the same category.
- It encodes both images and texts into **embedding** vectors in a shared latent space.
- For product  $j$ , having image  $M_j$  and text  $T_j$ , I get,

$$e_M(M_j) \in \mathbb{R}^{512}$$

$$e_T(T_j) \in \mathbb{R}^{512}$$

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<sup>7</sup>Chia et al., 2022, Nature Scientific Reports: Trained on 700,000 pairs from Farfetch, one of the largest fashion luxury retailers in the world.

# Validation 1: Predictive Performance of Image Embeddings

Image embeddings can predict sales and prices.

$$y_j = f(e_M(M_j)) + \epsilon_j$$

Model $f$	R2 Scores for Log Shares		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.69	0.27	0.69	0.33
Ridge	0.68	0.31	0.69	0.37
Random Forests	0.87	0.43	0.86	0.41
Deep Nets	0.87	0.44	0.62	0.46
Boosting Machine	0.88	0.45	0.89	0.48
Ensemble	0.89	0.47	0.79	0.49

## Validation 2: Predictive Performance of Text Embeddings

Text embeddings can predict sales and prices.

$$y_j = f(e_T(T_j)) + \epsilon_j$$

Model $f$	R2 Scores for Log Shares		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.59	0.0	0.76	0.39
Ridge	0.57	0.08	0.74	0.47
Random Forests	0.77	0.34	0.85	0.63
Deep Nets	0.72	0.20	0.68	0.56
Boosting Machine	0.78	0.34	0.87	0.67
Ensemble	0.77	0.33	0.79	0.64

# Validation 1: Predictive Performance of Combined Embeddings

Combining information does even better.

$$y_j = f(e_M(M_j), e_T(T_j)) + \epsilon_j$$

Model $f$	R2 Scores for Log Shares		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.85	0.04	0.88	0.26
Ridge	0.83	0.26	0.87	0.42
Random Forests	0.88	0.47	0.90	0.59
Deep Nets	0.94	0.38	0.77	0.49
Boosting Machine	0.90	0.49	0.92	0.63
Ensemble	0.93	0.51	0.92	0.67

## Validation 4: Visualizing the Product Space

I use tSNE<sup>8</sup> to reduce to two dimensions:  $e_{tSNE}(e_M(M_j), e_T(T_j)) \in \mathbb{R}^2$   
and then detect 24 clusters<sup>9</sup>.



<sup>8</sup>t-distributed Stochastic Neighbour Embedding

<sup>9</sup>Each dot is a dress, and each image is the most representative dress in that cluster.

# Validation 5: Within Cluster Variation

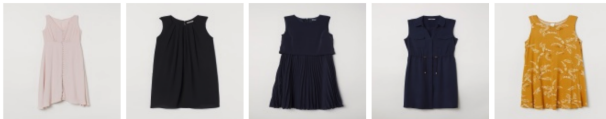
Word Cloud for Cluster 1 (122 articles)

sleeveless line dress

short sleeveless line

dress cr pe weave

dress woven fabric  
short sleeveless dress



Word Cloud for Cluster 13 (57 articles)

neck long sleeves

sleeves seam waist  
long sleeves seam

short lace dress

lace dress neck



Word Cloud for Cluster 16 (81 articles)

shoulder dress airy

short wide sleeves

elastication short wide

dress elastication short  
length shoulder dress



# Validation 5: Within Cluster Variation

Word Cloud for Cluster 23 (119 articles)

gathered seam waist  
length dress airy  
calf length dress

dress airy patterned

cuffs gathered seam



Word Cloud for Cluster 10 (147 articles)

adjustable shoulder straps

calf length dress  
narrow adjustable shoulder  
neck narrow adjustable  
dress woven fabric



Word Cloud for Cluster 8 (99 articles)

short puff sleeves  
puff sleeves narrow  
dress woven fabric

calf length dress

short line dress

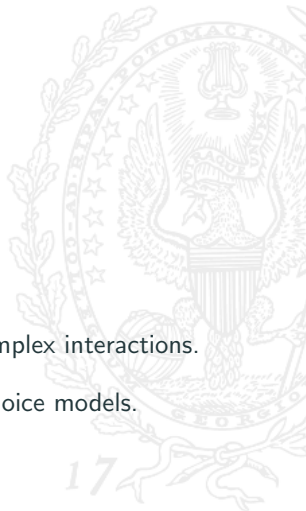


# Main Takeaways

This section shows that:

- Embeddings represent images and text well:
  - They are predictive of sales and prices
  - They cluster products intuitively.
- OLS cannot extract insights from embeddings.
- Deep networks do better because they allow complex interactions.

In the next section, I incorporate embeddings into choice models.





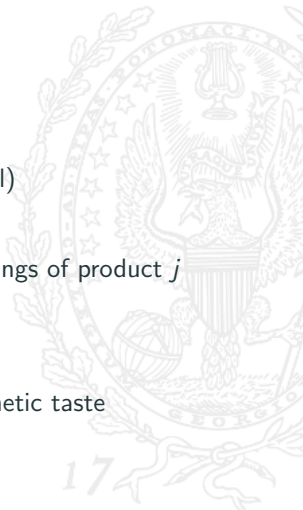
# Consumer Choice Models

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Key terms:

- $y_i$  Product purchases by consumer  $i$  (Categorical)
- $p_j$  Avg Price of product  $j$
- $X_j = [e_M(M_j), e_T(T_j)]$  Text and Image Embeddings of product  $j$
- $D_i$  Demographics of consumer  $i$
- $\alpha, \alpha^{DNN}$  Price Parameter
- $g^{DNN}$  Deep Neural Network that measures aesthetic taste



# Consumer Choice Model

For  $i$ -th consumer the utility given by the  $j$ -th product is given by,

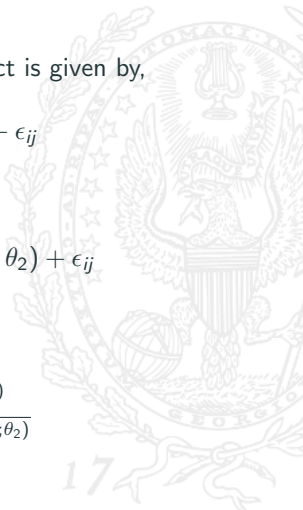
$$u_{ij} = h_1(p_j, D_i; \theta_1) + h_2(X_j, D_i; \theta_2) + \epsilon_{ij}$$

and discrete choice is,

$$y_i = \operatorname{argmax}_{j \in \{1, 2, \dots, J\}} h_1(p_j, D_i; \theta_1) + h_2(X_j, D_i; \theta_2) + \epsilon_{ij}$$

If  $\epsilon_{ij}$  is EV(1) and IID,

$$\mathbb{P}(y_i = j) = \frac{e^{h_1(p_j, D_i; \theta_1) + h_2(X_j, D_i; \theta_2)}}{\sum_k e^{h_1(p_k, D_i; \theta_1) + h_2(X_k, D_i; \theta_2)}}$$



This leads to the loglikelihood:

$$\ell(\theta) = \sum_i \sum_j \mathbf{1}(y_i = j) \log \left( \frac{e^{h_1(p_j, D_i; \theta_1) + h_2(X_j, D_i; \theta_2)}}{\sum_k e^{h_1(p_k, D_i; \theta_1) + h_2(X_k, D_i; \theta_2)}} \right)$$

- Estimation: get  $\ell'(\theta)$  (backdrop) + hill climbing
- StdErr: Hessians + Influence functions (Farell et al., 2018, 2021)
- No outside good! Model limited to consumers who do purchase.

I estimate models from simple to complex:

- $u_{ij} = \alpha \log p_j + \beta' X_j + \epsilon_{ij}$
- $u_{ij} = \alpha \log p_j + g^{DNN}(X_j) + \epsilon_{ij}$
- $u_{ij} = \alpha \log p_j + g^{DNN}(X_j, D_i) + \epsilon_{ij}$
- $u_{ij} = \alpha' d_i \log p_j + g^{DNN}(X_j, D_i) + \epsilon_{ij}$
- $u_{ij} = \alpha^{DNN}(D_i) \log p_j + g^{DNN}(X_j, D_i) + \epsilon_{ij}$



## Results I: Controls Matter

Model	$\alpha$	Std Err	p-value
$u_{ij} = \alpha \log p_j + \beta' X_j + \epsilon_{ij}$	-0.40	0.02	0.00
$u_{ij} = \alpha \log p_j + g^{DNN}(X_j) + \epsilon_{ij}$	-0.26	0.02	0.00
$u_{ij} = \alpha \log p_j + g^{DNN}(X_j, D_i) + \epsilon_{ij}$	-0.37	0.02	0.00

**Table 1:** Homogenous Logit Results

## Results II: Heterogenous Price Sensitivity

$$u_{ij} = (\alpha' D_i) \log p_j + g^{DNN}(X_j, D_i) + \epsilon_{ij}$$

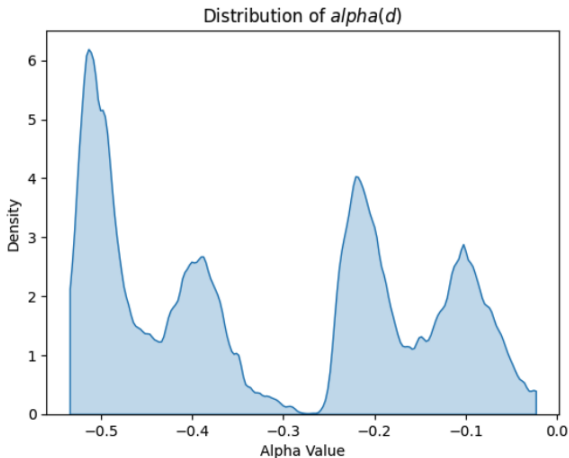
Standardized Variable	Coefficient
Intercept	-0.4249
Active Communications	-0.1551
Age	-0.0428
Club Member Active	-0.1427
Club Member Left	-0.1374
Club Member Processing	0.0976
Following Newsletter	0.3864
News Freq Monthly	0.0928
News Freq None	0.2663
News Freq Regularly	0.0343

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## Results III: Heterogenous Price Sensitivity

Neural networks capture a larger heterogeneity in price sensitivity.

$$u_{ij} = \alpha^{DNN}(D_i) \log p_j + g^{DNN}(X_j, D_i) + \epsilon_{ij}$$





## Results IV: Heterogenous Consumer Aesthetics

Using the  $g$  function, I rank order all products for two groups of people.



**Figure 1:** Top ranked dresses for 95th quantile by age (55-60)



**Figure 2:** Top ranked dresses for 5th quantile by age (18-21)

# Main Takeaways

Some insights from choice models:

- Price sensitivities can range widely:
  - **A 50% percent discount increases probability of purchase for some by 25% and others by only 5%.**
- **Different demographics have very different aesthetic tastes.**



Some enrichments:

- Richer demographics.
- Brand loyalty.
- Seasonal variation.
- Unobserved heterogeneity.
- Price endogeneity.



# Seasonal Variation and Unobserved Types

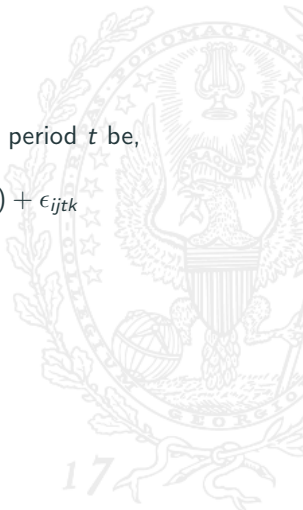
Utility for  $j$ -th product for  $i$ -th customer of type  $k$  in period  $t$  be,

$$U_{ijtk} = \alpha_k(D_i, S_t) \log p_{jt} + g_k(X_j, D_i, S_t) + \epsilon_{ijtk}$$

$p_{jt}$  Prices

$S_t$  Seasonal Dummies

$k$  Unobserved Type



# Seasonal Variation and Unobserved Types

Allowing unobserved types of consumers helps account for missing demographic information<sup>10</sup>:

$$\mathbb{P}(y_i = j) = \sum_k \pi_k \frac{e^{\alpha_k(D_i, S_t) \log p_{jt} + g_k(X_j, D_i, S_t)}}{\sum_{j'} e^{\alpha_k(D_i, S_t) \log p_{j't} + g_k(X_{j'}, D_i, S_t)}}$$

- Additional parameters to estimate:  $\pi_k, \alpha_k, g_k$
- Choice of  $k$ : when the likelihood increases tapers off.

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<sup>10</sup>Heckman and Singer 1984

# Handling Price Endogeneity via Control Functions<sup>13</sup>

Given instruments  $Z_{jt}$ <sup>11</sup> we have,

$$u_{ijt} = \alpha \log p_{jt} + g(X_j, S_t) + \xi_{jt} + \epsilon_{ijt}$$

where  $\xi_{jt}$ <sup>12</sup> is the omitted variable. We model  $\xi_{jt}$ ,

$$\log p_{jt} = q(X_j, S_t, Z_{jt}) + v_{jt}$$

$$\xi_{jt} = \gamma(v_{jt})$$

This gives us,

$$\mathbb{P}(y_i = j) = \frac{e^{\alpha \log p_{jt} + g(X_j, S_t) + \xi_{jt} + \epsilon_{ijt}}}{\sum_{j'} e^{\alpha \log p_{j't} + g(X_{j'}, S_t) + \xi_{j't} + \epsilon_{ij't}}}$$

<sup>11</sup>Lagged prices, lagged shares, BLP, differentiation, costs, Wagelfold, Hausman.

<sup>12</sup>Promotional activity (feature and display), word-of-mouth effects

<sup>13</sup>Villas-Boras and Winer 1999, Petrin and Train 2010

# Simulations

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- Optimal Discounts:

- Given budget  $B$ , set of customers arriving  $T_i$ , assuming costs  $c_j$ , how do we select discounts  $w_{ij}$ :

$$\mathbf{w} = \operatorname{argmax}_{w_{ij}} E\left[\sum_{i \in T_i} \sum_j 1(y_i = j)(p_j - w_{ij} - c_j)\right]$$

$$\sum_i \sum_j w_{ij} = B$$

- If nonlinear logit is true, what is the profit lost in using simple logit?
- What is the welfare cost of discounts?
- Can price discrimination actually help some section of consumers?

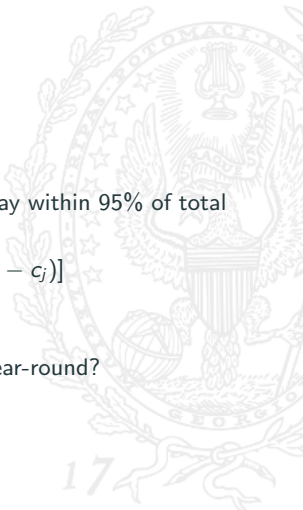


- Optimal Number of Designs:

- How many designs does H&M really need to stay within 95% of total profits?

$$\pi = \max E\left[\sum_{i \in T_i} \sum_j 1(y_i = j)(p_j - c_j)\right]$$

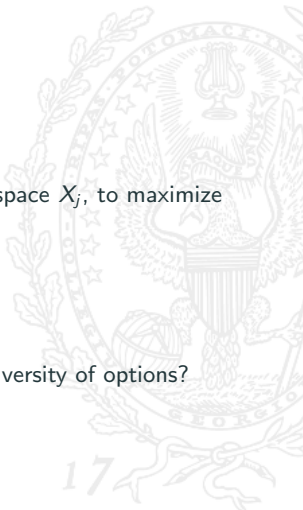
- Does H&M have too many designs?
- What if it just sold a core group of products year-round?



- Can AI design dresses?
  - Use optimization techniques to learn in latent space  $X_j$ , to maximize probability of purchase for a given consumer:

$$X_j^* = \operatorname{argmax}_{X_j} \mathbb{P}(y_i = j)$$

- What would be the total profit gain?
- What would AI-generated dresses reduce the diversity of options?



- Enrich the model:
  - Better demographics.
  - Brand loyalty.
  - Seasonal variation.
  - Unobserved Heterogeneity.
  - Price endogeneity.
- Conduct simulations:
  - Discounting.
  - Number of designs.
  - Using AI to develop designs.



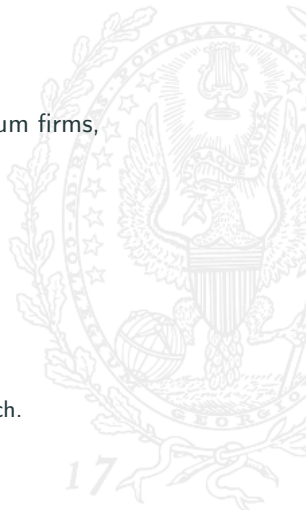
# Appendix

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- **Demand/Choice Models:** Train (2009), Gandhi and Houde (2019), Conlon and Gortmaker (2020), Berry and Haile (2021), Petrin and Train (2010)
- **Deep Learning Architectures:** Younesi et al., (2024), Vaswani et al., (2017), Kingma et al., (2015), LeCun et al., (2015), He et al., (2016), Sun et al., (2020).
- **Machine Learning in Econometrics:** Chernozhukov et al (2018, 2022), Farrell et al (2018, 2021), Ludwig & Mullainathan (2023).
- **Retail Fashion Industry:** McCormick et al (2014), Wen et al., (2019), Bhardwaj and Fairhurst (2009)
- **Applied Work:** Quah & Williams (2021), Han et al., (2021), Giovanni et al., (2021), Zhang et al (2022), He et al (2023), Janssens et al (2021), Zhang (2024)

- Monopolistic competition - many small to medium firms, differentiated products and few entry barriers.
- Fashion industry is characterized by:
  - large number of incomparable products.
  - short product lifespans.
  - large number of seasonal products.
  - collections with non-replishable inventory.
  - widespread promotions and discounts.
  - some amount of brand loyalty but not too much.



# Retail Fashion: Industry Evolution

Since the 1980s there have been critical changes<sup>14</sup>

- **Product Design:** End of mass-production (Levi's 501, White Tees) and move towards trendy and stylish apparel. This led to increase in mark-downs due to failure to sell inventory during season.
- **Fashion Seasons:** Shrinking of time between runway to delivery. Incorporation of 3-6 midseasons to the traditional fashion calendar (Spring/Summer + Autumn/Winter).
- **Supply Chain:** Cost reduction from outsourcing. Quick Response and Just-in-Time strategies to combat longer lead times, complex supply chains.
- **Consumers:** More aware of fashion trends, prices, and options. Increasingly interested in cheaper but fashionable clothes.

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<sup>14</sup>Bhardwaj and Fairhurst 2009

# Retail Fashion: Pricing

- Common methods to determine pricing:
  - Keystone markup - if costs are known then a simple markup is applied (2x, 4x).
  - Backwards pricing - find what consumers are willing to pay and then work back to determine cost and materials.
  - Promotion / Discounting - adjust prices to deplete inventory as season comes to an end.
- With better data, faster development to delivery times, smarter inventory management, there is more dynamic pricing.
- Fast fashion (Zara, HM), operate at scale, and have made average prices lower, but luxury brands (Dior, Chanel) have increased prices.



# Dresses: Worst Sellers

ID: 879646003  
Share: 0.00%



Short dress in a jacquard weave with a slight sheen. Double-layered stand-up collar and an opening at the back with concealed hook-and-eye fasteners at the back of the neck. Short, raglan puff sleeves with narrow elastication at the hems, and a seam at the waist with a narrow drawstring that ties at the back. Lined.

ID: 524855001  
Share: 0.00%



Pleated mesh dress that is transparent at the top with a small frilled collar and opening with a button at the back of the neck. Concealed zip in the side, a seam at the waist and a double-layered skirt. Lined.

ID: 577399004  
Share: 0.00%

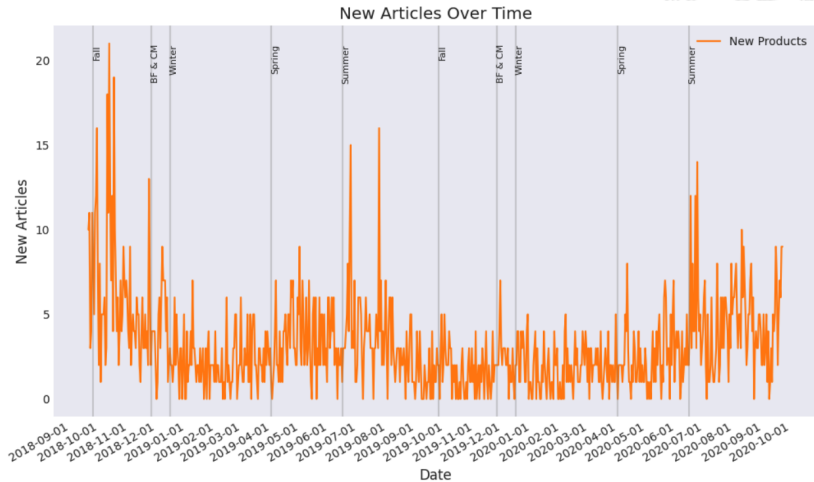


Shirt dress in a crêpe weave with a collar, button placket and short dolman sleeves. Yoke with a pleat at the back, and slits in the sides. Unlined.

17

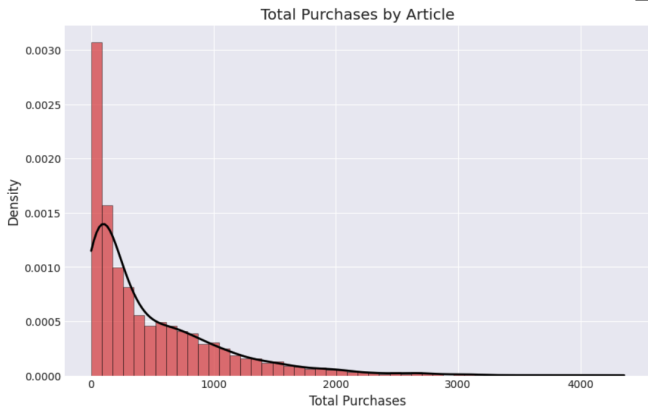
# Dresses: New Articles Launched

New dresses show up continuously over time.



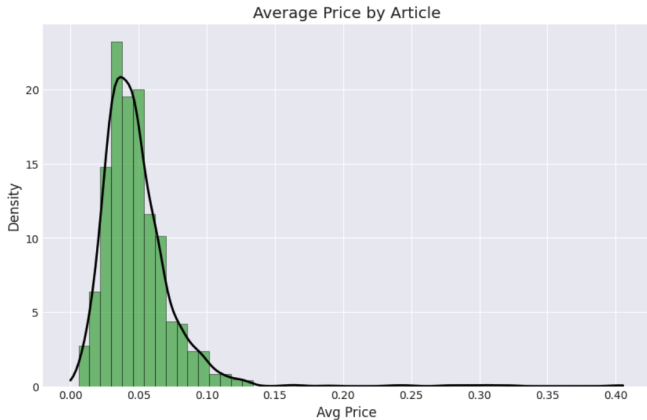
# Dresses: Distribution of Sales

A few dresses pick up a majority of the sales share.



# Dresses: Distribution of Prices

The price measure in the data has been scaled down.



# Model 1: Image Regression with CNN

I estimate a CNN model on raw image pixels to predict sales share:

$$s_j = g(M_j; \theta)$$

and get an out of sample R2 of approximately 0.35.

Original Image - Pred Share: 0.024%



Round Neck - Pred Share: 0.020%



Sleeveless - Pred Share: 0.032%



Occlusion can reveal how inputs map to outputs.

# RF Model 1: Counterfactuals

I use Dalle to generate images using the best seller as base to generate new designs. The predicted market shares are:

0.024%



0.003%



0.004%



0.003%



0.005%



0.008%



$$s_j = g(M_j; \theta)$$

## Additional Reduced Form Evidence

- Data  $\{M_j, p_j, s_j\}_{j=0}^J$  is split into training (80%) and test (20%) datasets
- Models tried: Linear Regression, Ridge, Random Forests, Neural Nets, Light Gradient Boosting, Ensemble
- Feature Sets:
  - 512 Image-embeddings:  $e(M_j)$
  - 495 TDIDF:  $t(T_j)$
  - 410 Sentence BERT:  $b(T_j)$
  - 1417 Image-embeddings + BERT + TDIDF:  $e(M_j), b(T_j), t(T_j)$
  - 50 Image-embeddings + BERT + TDIDF (factors):  
 $f[e(M_j), b(T_j), t(T_j)]$
- Regularization: L2 parameter 5.0 for Ridge and Neural Nets, `Min_samples_leaf = 10` for random forests and `min_data_leaf=100` for LGBM. Voting (Ensemble) averages neural net and LGBM.

# Product Usage

Features from customer demographics aggregated to product level.

**Table 2:** Log Sales and Prices on Product Usage

Model	R2 Scores for Log Sales		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.03	0.04	0.02	0.02
Ridge	0.01	0.01	0.00	0.00
Random Forests	0.41	0.20	0.33	-0.01
Deep Nets	0.00	0.01	-0.10	-0.08
LGBM	0.38	0.17	0.27	-0.02
Voting	0.25	0.15	0.16	0.01



# Product Categories

Large number of organizational dummies and other dummies related to product color, texture, etc.

**Table 3:** Log Sales and Prices on Product Categories

Model	R2 Scores for Log Sales		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.62	-7.05e+22	0.16	-3.79e+24
Ridge	0.59	0.61	0.14	-0.04
Random Forests	0.58	0.60	0.17	0.01
Deep Nets	0.64	0.62	0.07	-0.01
LGBM	0.41	0.40	0.10	-0.03
Voting	0.56	0.56	0.09	-0.01

Image-Em

**Table 4:** Log Sales and Prices on Image Features

Model	R2 Scores for Log Sales		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.68	0.22	0.69	0.29
Ridge	0.65	0.38	0.66	0.42
Random Forests	0.78	0.43	0.76	0.41
Deep Nets	0.66	0.45	0.55	0.45
LGBM	0.89	0.46	0.88	0.42
Voting	0.82	0.49	0.76	0.47

**Table 5:** Log Sales and Prices on BERT Features

Model	R2 Scores for Log Sales		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.72	0.38	0.27	-0.44
Ridge	0.38	0.29	0.06	-0.03
Random Forests	0.83	0.59	0.43	-0.11
Deep Nets	0.35	0.26	0.02	-0.01
LGBM	0.92	0.69	0.52	-0.19
Voting	0.73	0.55	0.34	-0.04

Table 6: Log Sales and Prices on TFIDF Features

Model	R2 Scores for Log Sales		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.73	-1.54e+20	0.27	-3.78e+19
Ridge	0.57	0.46	0.12	-0.05
Random Forests	0.74	0.57	0.33	-0.06
Deep Nets	0.56	0.45	0.03	-0.01
LGBM	0.76	0.56	0.35	-0.07
Voting	0.69	0.53	0.22	-0.01

**Table 7:** Log Sales and Prices on All Features

Model	R2 Scores for Log Sales		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.99	-0.77	0.95	-4.61
Ridge	0.88	0.72	0.75	0.39
Random Forests	0.86	0.65	0.77	0.39
Deep Nets	0.83	0.70	0.58	0.45
LGBM	0.95	0.71	0.90	0.43
Voting	0.91	0.74	0.78	0.47

# All Features Compressed

Factor analysis is used to compress features to 50 dimensions.

**Table 8:** Log Sales and Prices on All Features Compressed to 50

Model	R2 Scores for Log Sales		R2 Scores for Log Prices	
	Train	Test	Train	Test
OLS	0.56	-1.17e+10	0.39	-3.70e+11
Ridge	0.56	0.53	0.39	0.35
Random Forests	0.75	0.49	0.66	0.33
Deep Nets	0.83	0.59	0.43	0.36
LGBM	0.83	0.55	0.76	0.34
Voting	0.84	0.60	0.63	0.37

# Attention-Based Embeddings

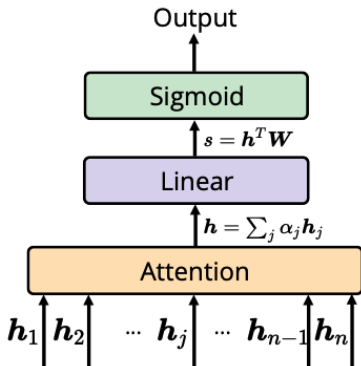
Moving beyond word counting, we need to understand how words interact in a given context:

- **Text Description:**  $T = (w_1, w_2, w_3, \dots, w_N)$
- **Word Embeddings:**  $e_W(T) = (h_1, h_2, h_3, \dots, h_N)$
- **Attention Weight:**  $\alpha_n = \frac{\exp\{h_n^T V / \lambda\}}{\sum_{n'} \exp\{h_{n'}^T V / \lambda\}}$  tells us the importance of word  $w_n$  in determining the “context” of the entire description  $T$ .
- **Context:**  $h = \sum_n \alpha_n h_n$  A high dimensional representation of the entire text  $T$ , which allows us to differentiate the text along multiple “attributes”.
- **Scaler Prediction:**  $s = h^T W$  picks up relevant contexts.

Trainable parameters: query weights  $V$ , context weights  $W$ .

# Attention-Based Embeddings

The high dimensional context layer  $h = e(T)$  will now represent our entire text  $T$ .



We can train this ourselves, or use a pre-trained model.





## Model 3: Text Regression with Word Counts

I generate dummies from the text based on n-grams and estimate a Ridge regression on log sales to get an out of sample **R<sup>2</sup>: 0.37**.

### Top 10 $\beta$

1. crêpe weave neck
2. neckline
3. viscose
4. sheen opening
5. wide flounce hem unlined
6. short fitted dress velour
7. buttons short
8. calf length dress
9. neck rounded
10. sleeves smocking

### Bottom 10 $\beta$

1. straight
2. tie
3. dress
4. short dress satin
5. unlined
6. elasticated cuffs
7. appliqués
8. striped
9. seam waist slit
10. shoulder dress



## Model 3: Variation by Age

Keyword significance varies across age groups, emphasizing diverse product preferences. “Young” is below 21, and “old” is above 60.

### All ( $R^2 = 0.37$ )

- crêpe weave neck
- neckline
- viscose
- sheen opening
- wide flounce hem unlined

### Young ( $R^2 = 0.38$ )

- short dress
- cuffs
- long wide sleeves
- opening narrow ties
- opening narrow

### Old ( $R^2 = 0.54$ )

- viscose
- viscose weave neck
- wide flounce hem unlined
- buttons short
- shoulder straps buttons

## Model 3: Machine Learning Methods

Moving beyond linear models, I find that nonlinear models can better extract generalizable signals.

**Table 9:** R2 Scores for Models on Log Shares

Model	R2 Train	R2 Test
OLS	1.00	0.00
Ridge	1.00	0.66
Random Forests	0.76	0.59
Deep Nets	0.98	0.75
Boosting Machines	0.77	0.59
Ensemble	0.93	0.74

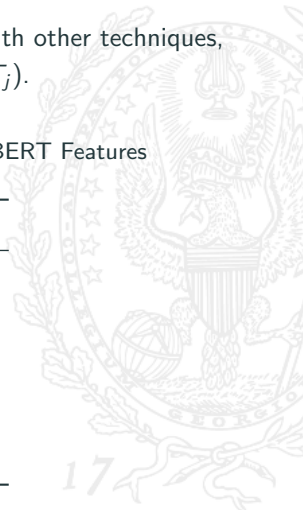
Due to large covariate set ( $\geq 10,000$ ), OLS completely overfits.

## Model 4: Sentence BERT

Sentence-BERT uses attention mechanisms, along with other techniques, to create 410 dimensional sentence embeddings  $e_B(T_j)$ .

**Table 10:** R2 Scores for Log Sales on Sentence-BERT Features

Model	Train	Test
OLS	0.73	0.40
Ridge	0.73	0.42
Random Forests	0.83	0.61
Deep Nets	0.95	0.66
Boosting	0.92	0.68
Ensemble	0.96	0.72



# Model 4: Visualization

I discover natural “topics” in the text embedding through clustering and find representative images for them.

sleeves  
back  
short  
dress  
waist



kneelength  
dress  
unlined  
waist  
sleeves



calflength  
front  
seam  
dress  
waist



seam  
dress  
chiffon  
gathered  
airy  
back



back  
dress  
short  
crepe  
weave



sleeves  
vneck  
tunic  
short



added  
aline  
elastication  
dress  
short



jersey  
top  
panels  
silicone  
bandeau  
support  
offtheshoulder  
elastication



lined  
maxi  
seam  
double



# tSNE and Kmeans Clustering

I compress the 512-dim image embeddings into 2 dimensions via t-SNE and find clusters:

- **t-SNE (t-distributed Stochastic Neighbor Embedding):**

- Reduces dimensions by minimizing the Kullback-Leibler divergence between two distributions:
- $C = KL(P||Q) = \sum_i \sum_j p_{ij} \log \frac{p_{ij}}{q_{ij}}$
- $p_{ij}$  - probability of picking  $j$  as neighbor of  $i$  in high-dimensional space.
- $q_{ij}$  - probability in the low-dimensional embedding.

- **K-Means Clustering:**

- Objective is to partition  $n$  observations into  $k$  clusters by minimizing within-cluster variances:
- $J = \sum_{i=1}^k \sum_{x \in S_i} \|x - \mu_i\|^2$
- $\mu_i$  is the mean of points in  $S_i$ .

# Autoencoders

We want to compress  $e_O(M_j), e_B(T_j)$  without losing too much information (e.g. tSNE):

- **Autoencoders:** Estimate a neural network to predict  $e_O(M_j), e_B(T_j)$  from itself, and use hidden layer outputs.
  - **Input** data:  $\mathbf{x} = [e_O(M_j), e_B(T_j)]$
  - **Encoder** function:  $\mathbf{f}$  (high dim to low dim)
  - **Decoder** function:  $\mathbf{r}$  (low dim to high dim)
- **Reconstruction Loss:** Mean squared error (MSE)

$$L(\mathbf{x}, \mathbf{f}, \mathbf{r}) = \|\mathbf{x} - \mathbf{r}(\mathbf{f}(\mathbf{x}))\|^2 \quad (1)$$

- **Latent Space:** The encoder maps the input to the latent space  $\mathbf{f}(\mathbf{x})$  (hidden representation), which the decoder then uses to reconstruct the input.

I compress the image + text embeddings into 100 dimensions:

$X_j = f(e_O(M_j), e_B(T_j))$  for structural modelling.

# Market Demand

For  $J$  products and  $N$  individuals, we have utilities given by,

$$u_{ij} = \alpha \log p_j + g(X_j) + \xi_j + \epsilon_{ij}$$

$$X_j = f(e_O(M_j), e_B(T_j))^{15}$$

this gives rise to market demand,

$$\log s_j = \log s_0 + \alpha \log p_j + g(X_j) + \xi_j$$

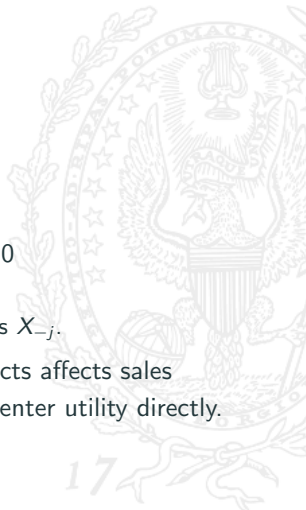
$y_{ij}$	Purchase of $j$ product by consumer $i$	$e_O, e_B$	Embedding Layers
$p_j$	Price of product $j$	$\alpha$	Price Elasticity
$M_j$	Image of product $j$	$f$	Autoencoder Layer
$T_j$	Text of product $j$	$\epsilon_{ij}$	IID Gumbel Error
$s_j$	Sales share of product $j$	$\xi_j$	Market demand shock

<sup>15</sup>I use autoencoders for compressing embeddings into 100 dimensions



# Market Demand: Assumptions

- Utility is linearly separable and  $\epsilon_{ij}$  is IID.
- Endogenous Prices:  $\xi_j \not\perp p_j | (M_j, T_j)$
- Exogenous Characteristics:  $\xi_j \perp (M_j, T_j)$
- We have  $K \times 1$  instruments such that  $E[\xi_j Z_{jk}] = 0$ 
  - Differentiation IVs: Distances between  $X_j$
  - BLP IVs: Sums of other product characteristics  $X_{-j}$ .
- Instrument logic: Proximity to competing products affects sales through reduced markups (prices) but does not enter utility directly.



# Market Demand: Estimation

Here we draw from the debiased machine learning literature (Chernozhukhov et al., 2016, 2018):

- Partially Linear Regression (PLR):
  - $y_j = \theta T_j + g(X_j) + \epsilon_j$
  - $E[\epsilon_j | T_j, X_j] = 0$
- Partially Linear Instrumental Variables (PLIV)
  - $y_j = \theta T_j + g(X_j) + \epsilon_j$
  - $E[\epsilon_j | Z_j, X_j] = 0$
- Estimation:
  - ML + regularization used to approximate  $g$ .
  - First stage: Partial out  $[X, Z]$  from  $T$  and  $y$  using dataset  $A$
  - Second stage: Regress residuals on data  $B$  to estimate  $\alpha$



# Market Demand: Results

$y_j$ : log shares,  $\log s_j$      $T_j$ : log prices,  $\log p_j$      $X_j$ : Autoencoded Embeddings

**Table 11:** Coefficient Table

Model	OLS	PLR	IV	PLIV
$\alpha$	-0.54	-0.41	-0.84	-0.52
Std. Error	0.08	0.08	0.17	0.18
t-value	-7.13	-4.95	-4.88	-2.89
p-value	0.00	0.00	0.00	0.00
LB 0.025	-0.69	-0.57	-1.18	-0.88
UB 0.975	-0.39	-0.25	-0.50	-0.17
N	2319	2319	2319	2319

First stage with LGBMRegressor showed train R2 0.83, test R2 0.67; PLR & PLIV used 5-fold cross splitting and LGBM to estimate  $g$  with 100 min\_data\_leaf.

# Consumer Choice: Inference

Farell et al., (2019, 2021) show that inference can be done by deep nets:

- Parametric Loss:  $\theta(x) = \operatorname{argmin}_{\theta} E[L(Y, T, \theta(X))]$ 
  - $\theta(x) = \operatorname{argmin}_{\theta} E[L(Y, T, \theta(X))]$
  - Exp. Hessian:  $\Lambda(x) = E[L_{\theta\theta}|X, T]$
- Inference Target:  $\mu = E[H(X, \theta(X); T = t^*)]$
- Influence Function:  $\Psi(y, t, x) = H - H_{\theta}\Lambda(x)^{-1}L_{\theta}$ 
  - Measures the change in target  $\mu$  for a infinitesimal change in observation  $(y, t, x)$ .
- Estimation:
  - Deep neural networks  $\hat{\theta}(x)$  that minimize empirical loss.
  - $\hat{H}_{\theta}, \hat{L}_{\theta}, \hat{\Lambda}(x_i)$  obtained by automatic differentiation.
- Inference:
  - From  $\hat{\theta}(x_i), \hat{\Lambda}(x_i)$  get  $\hat{\Psi}(y_i, t_i, x_i)$ .
  - $\hat{\mu} = \frac{1}{n} \sum_i \hat{\Psi}(y_i, t_i, x_i)$
  - $\widehat{\operatorname{Avar}}(\hat{\mu}) = \frac{1}{n} \sum_i (\hat{\Psi}(y_i, t_i, x_i) - \hat{\mu})^2$

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# Deep Logit: Simulation Study I

For  $J = 1000$ , I generate images  $M_j (J \times 3 \times 1024 \times 1024)$  from the MNIST Digits dataset. I generate  $u_{ij}$  according to,

$$u_{ij} = \log(1 + 0.1 \text{label}(M_j)) + \epsilon_{ij}$$

where label gives the actual digit value of the image of the digit.

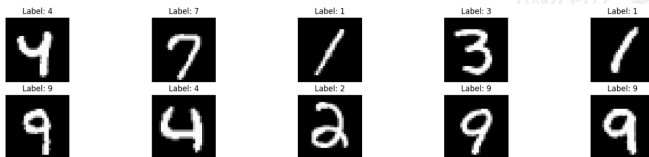


Figure 3: Product Images

# Deep Logit: Simulation Study II

I estimate model and check the average scores of  $\hat{g}(M_j)$  when  $\text{label}(M_j) = j$

$$u_{ij} = g(M_j) + \epsilon_{ij}$$

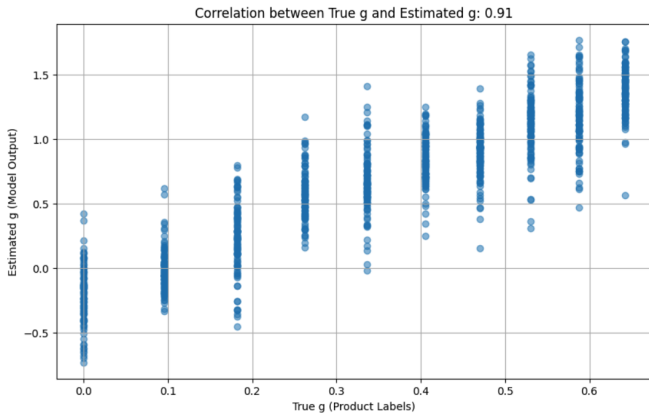


Figure 4: Product Images



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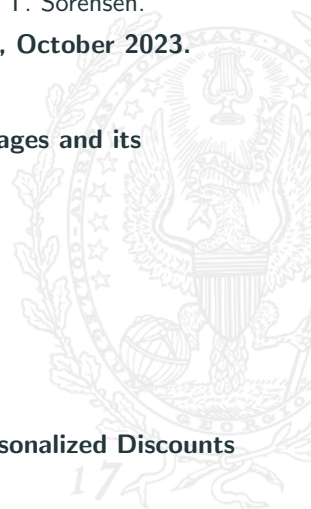




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